MEMORANDUM REPORT ARBRL-MR-02929 70 AD A 0 743 STATISTICS OF OPTICAL RADIATION SCATTERED FROM BOUGH SURFACES, Paul H./Deitz DDC Tommy E. Buder Jul 1979



US ARMY ARMAMENT RESEARCH AND DEVELOPMENT COMMAND
BALLISTIC RESEARCH LABORATORY
ABERDEEN PROVING GROUND, MARYLAND

16/14/16/11 \$ 2 AH 4/3

Approved for public release; distribution unlimited.

OUC FILE COP

393 471

79 09 12 028

Destroy this report when it is no longer needed. Do not return it to the originator.

Secondary distribution of this report by originating or sponsoring activity is prohibited.

Additional copies of this report may be obtained from the National Technical Information Service, U.S. Department of Commerce, Springfield, Virginia 22161.

The findings in this report are not to be construed as an official Department of the Army position, unless so designated by other authorized documents.

The use of trude names or manufacturers' names in this report does not constitute indorsement of any commercial product.

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE	READ INSTRUCTIONS BEFORE COMPLETING FORM	
1. REPORT NUMBER 2. GOVT ACCESSION NO.		
MEMORANDUM REPORT ARBRL-MR-02929		
4. TITLE (and Subtitle)	5. TYPE OF REPORT & PERIOD COVERED	
Statistics of Optical Radiation Scattered From Rough Surfaces		
Rough Surfaces	6. PERFORMING ORG. REPORT NUMBER	
7. AUTHOR(a)	B. CONTRACT OR GRANT NUMBER(*)	
Paul II. Deitz and Tommy E. Buder		
,		
9. PERFORMING ORGANIZATION NAME AND ADDRESS	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS	
US Army Ballistic Research Laboratory		
ATTN: DRDAR-BLB Aberdeen Proving Ground, MD 21005	RDTGE 1L161102AH43	
11. CONTROLLING OFFICE NAME AND ADDRESS	12. REPORT DATE	
US Army Armament Research & Development Command	JULY 1979	
US Army Ballistic Research Laboratory	13. NUMBER OF PAGES	
ATTN: DRDAR-BL, APG, MD 21005  14. MONITORING AGENCY NAME & ADDRESS(II dilterent from Controlling Office)	15. SECURITY CLASS (of this report)	
,	, , , , , , , , , , , , , , , , , , , ,	
	Unclassified	
	154, DECLASSIFICATION/DOWNGRADING SCHEDULE	
16. DISTRIBUTION STATEMENT (of this Report)		
Approved for public release; distribution unlimited		
17. DISTRIBUTION STATEMENT (of the abetract entered in Black 20, if different fro.	m Report)	
18. SUPPLEMENTARY NOTES		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number)	Į.	
Gun erosion Speckle pattern Surfac Optical scattering Laser illumi	e roughness	
sperall bouttering mastriffully	nacron .	
20. ABSTRACT (Continue on reverse side if necessary and identify by block number)	(hms)	
When coherent illumination is scattered from a re	(hmn)	
pattern or light (speckle pattern) has stochastic variations in irradiance which l		
relate to the scattering surface itself. A computer simulation for a particular		
scattering geometry has been made in which four star patterns have been related to various pairwise comb	tistical parameters of speckle	
correlation interval for a gaussian scattering surfa	ace. The corresponding	
optical analogue of this simulation has potential a	oplication to studies of gun	
crosion.		

## TABLE OF CONTENTS

		Page
	LIST OF FIGURES	5
I.	INTRODUCTION	7
II.	PROBLEM FORMULATION	?
III.	RESULTS OF CALCULATIONS	Ģ
IV.	CONCLUSIONS	12
	DISTRIBUTION LIST	

The second secon	
Accession For	
NTIS GRAEI DDC TAB Unannounced	
Justification	
Ву	
Distribution/ Avoil:bility Codes	
[423] 800/01	
Dist special	

# LIST OF FIGURES

Figure		Page
1	Setup for generation of optical scattering pattern	7
2	Computer-generated gaussian phase surface	8
3	Expected irradiance vs. surface roughness and correlation interval	9
4	Expected standard deviation vs. surface roughness and correlation interval	10
5	Expected RMS/AVE ratio vs. surface roughness and correlation interval	10
6	Expected correlation interval vs. surface roughness and correlation interval	11



#### Ι. INTRODUCTION

When a laser beam is used to illuminate a rough surface, the resulting scatter pattern takes on a random, mottled character. This pattern is usually referred to as a speckle pattern, and its statistics relate not only to the particular radiance pattern on the surface of the scatterer but to the surface roughness as well. For another investigation, a computer program was written to evaluate numerically the far-field scatter pattern due to coherent illumination from a one-dimensional surface characterized by gaussian statistics. For that particular study, the statistics of the speckle pattern were examined with respect to the form of the radiance distribution over the scattering surface.

This present investigation was prompted by a problem related to gun erosion. Central to the estimation of gun tube wear is the assessment of surface roughness from one firing to the next. With a view toward developing an experimental technique useful in the analysis of surface structure, we utilized our one-dimensional analytical model to examine the relationship between roughness at a scattering surface and certain statistics of the scattered radiation.

#### PROBLEM FORMULATION

An attempt was made to model a scattering geometry which might be used in an actual measurement. With this in mind, an object 1 mm in length was chosen with radiation at 0.6-micron wavelength. The geometry is shown in Figure 1. The line source formed the input to a 15-cm focal length lens. At the output focal line, the speckle field was evaluated using the Huygens-Fresnel equation. The integral form of this equation describes the output field as an integral over the input aperture, where

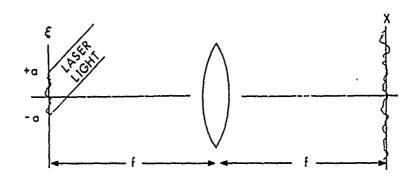


Figure 1. Setup for generation of optical scattering pattern. Laser light impinges on surface at & plane. Radiation is transformed by lens to plane X. The problem is to relate the statistics of the optical radiation at plane X to the surface characteristics in plane  $\xi$ .

R. Barakat, P.H. Deitz and T.E. Buder, "A New Class of Communications Systems: II. Theory", BRL Memorandum Report to be published.

$$V(x) \propto \int_{-2}^{\hat{a}} V(\xi) \exp \left[-i \frac{2\pi}{\lambda f} x \xi\right] d\xi, \qquad (1)$$

Here, V(x) is the output field, the limits of integration are from -a to a where a is  $^{1}_{2}$  mm,  $V(\xi)$  is the complex scattered field at the rough surface,  $\lambda$  is the wavelength of the radiation, and f is the focal length of the lens.

In our evaluation, a special subroutine was used which generates stochastic functions which are gaussian in nature and conform to chosen parameters of standard deviation (vertical surface structure) and correlation interval (average scale size along the surface). Since the illuminated spot is small, a constant amplitude was assumed within the scattering aperture so that the statistics of the scattered radiation were a function of phase only. Figure 2 shows one computer realization of the phase of the optical beam immediately after scatter at the rough surface for one set of parameters. The standard deviation is one-tenth of a wavelength and the correlation interval is 5 microns.

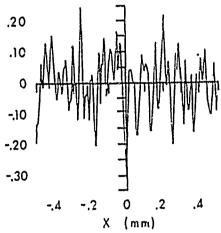


Figure 2. Computer-generated guassian phase surface having standard deviation (sigma) of 0.1 lambda (where lambda (L) is 0.6 microns) and a correlation interval (alpha) of five microns.

Equation (1) was utilized in discrete form for 400 equally spaced points across the 1-mm object and evaluated at 400 locations in the detection plane over a distance of 40 cm. After the 400 complex field calculations were made in the detection plane, the results were squared to give the measurable quantity, the intensity pattern.

For the gun erosion application, a range of height-roughness variations from 0 to 0.9  $\lambda$  (in standard deviation), where  $\lambda$  is the wavelength, were examined together with correlation interval variations from 5 to 105 microns. Six particular values of standard deviation were used with five values for the correlation interval in every possible pairwise combination. For each of these 30 pairs of parameters, 15 realizations of the radiation pattern in the detection plane were generated. Various statistical parameters were extracted from these speckle patterns and are discussed in the next section.

#### III. RESULTS OF CALCULATIONS

Using the 15 realizations of speckle pattern for each of 30 pairs of surface height (sigma) correlation interval (alpha), four specific statistical variables were examined: mean irradiance, standard deviation, ratio of RMS/average, and the correlation interval.

For each of the four statistical parameters examined, the procedure was similar. The parameter under evaluation was computed for each speckle pattern and then averaged over the 15 realizations computed for each of the 30 pairs of sigma/alpha variables. Standard deviations about these means were also computed to give an indication of the statistical uncertainty. Figure 3 gives the expected value of the speckle

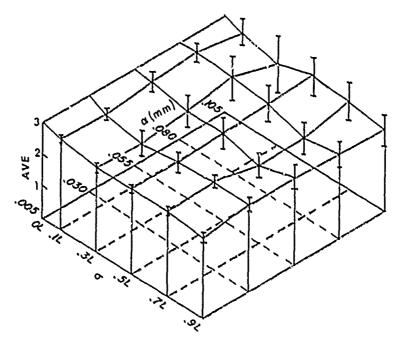


Figure 3. Three-dimensional perspective plot showing expected value of average irradiance of scattering pattern vs. pairwise combinations of surface height (sigma) and correlation interval (alpha) of illuminated surface. L is the wavelength of the optical illumination (0.6 microns). Each point represents the expected value of 15 realizations of a speckle pattern for which the average value has been computed. Error bars indicate the one-sigma variations about the expected value. Absence of error bars indicates a nonstochastic calculation.

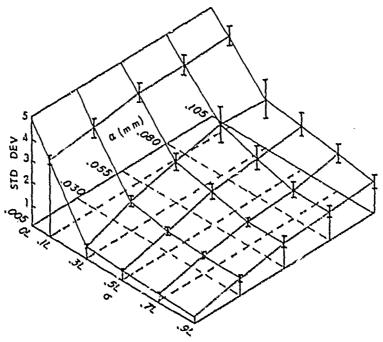


Figure 4. Perspective plot showing expected value of standard deviation vs. pairwise combinations of surface height (sigma) and correlation interval (alpha) of scattering surface.

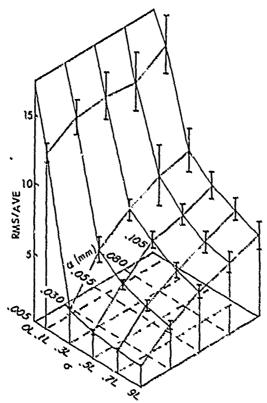


Figure 5. Perspective plot showing expected value of RMS/AVE ratio vs. pairwise combinations of surface height (sigma) and correlation interval (alpha) of scattering surface.

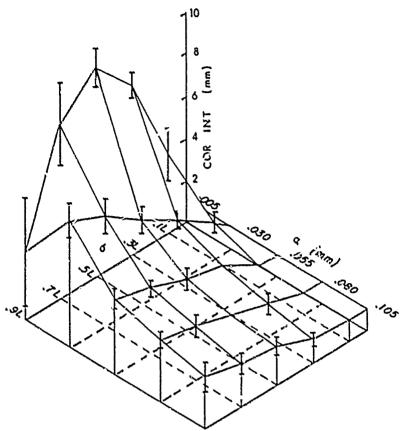


Figure 6. Perspective plot showing expected value of corrolation interval (in mm) vs. pairwise combinations of surface height (sigma) and correlation interval (alpha) of scattering surface.

irradiance (in relative units) versus various sigma/a.phas. As might be expected, the mean is essentially independent of surface structure. Bars above and below the mean values indicate the one-sigma values based on 15 realizations. An imprease in the correlation interval gives a greater uncertainty in the value of the expected irradiance. Absence of error bars indicates a nonstochastic calculation.

Figure 4 gives the results for the standard deviation of speckle statistics versus the pair-wise independent parameters. Standard deviations are generally higher for low surface standard deviation and/or large correlation interval. Figure 5 shows the ratio of RMS surface roughness to average. This ratio follows the same trend as the standard deviation given in Figure 4. This result is to be expected since the standard deviation and RMS are essentially identical computations for a large sample size, and the mean here is relatively constant.

Finally, Figure 6 gives the expected correlation interval (in mm) as a function of the sigma-alphas. This function goes through a noticeable peak for a small correlation interval of surface roughness and the midrange of surface standard deviation.

#### IV. CONCLUSIONS

The surface shapes suggested by Figures 4-6 indicate that it may be possible to associate specific scatter statistics with particular surface parameters. The central problem is to associate a unique set of surface conditions with a particular statistic in the measured speckle pattern. From these results, it can be seen that specification of, for example, a particular ratio of RMS/AVE value does not relate to just one, but a restricted set of alpha-sigma pairs. However, the combined use of both the RMS/AVE results (Figure 5) together with the correlation interval calculations (Figure 6) would help reduce the number of sigma/alpha pairs which can result in the same scattering statistics. Further, if it can be argued on physical grounds that the correlation interval and the surface height of the scattering surface must be correlated in some way, then the ambiguity in the interpretation of the scattering data might further be reduced.

From such optical scattering experiments as those described here, it might then be possible to relate a series of speckle measurements to a specific set of surface roughness characteristics.

DISTRIBUTION LIST			
No. of Copies Organization	No. of Copies Organization		
12 Commander Defense Documentation Center ATTN: DDC-DDA Cameron Station Alexandria, VA 22314	1 Commander US Army Electronics Research and Development Command Technical Support Activity ATTN: DELSD-L Fort Monmouth, NJ 07703		
1 Director Defense Advanced Research Project Agency Tactical Technical Office ATTN: Dr. James Tegnelia 1400 Wilson Boulevard Arlington, VA 22209	1 Commander US Army Communications Rsch and Development Command ATTN: DRDCO-PPA-SA Fort Monmouth, NJ 07703		
1 Director Institute for Defense Analysis ATTN: Dr. Bruce J. Whittemore 400 Army Navy Drive Arlington, VA 22202	3 Commander US Army Harry Diamond Labs ATTN: DRXDO-TI DRXDO-SA, Mr. W. Pepper Mr. J. Salerno 2800 Powder Mill Road Adelphi, MD 20783		
1 Commander US Army Materiel Development and Readiness Command ATTN: DRCDMD-ST 5001 Eisenhower Avenue Alexandria, VA 22333 1 Commander	1 Director Office of Missile Electronic Warfare ATTN: DRSEL-WLH-SF, Mr. R. J. Clawson White Sands Missile Range, NM 88002		
US Army Aviation Research and Development Command ATTN: DRSAV-E P.O. Box 209 St. Louis, MO 63166	1 Commander US Army Night Vision and Electro-Optics Laboratory ATTN: DRSEL-NV-VI, Mr. J. Dehne Fort Belvoir, VA 22060		
US Army Air Mobility Research and Development Laboratory	2 Commander US Army Missile Research		

US Army Research & Technology

and Development Command

Redstone Arsenal, AL 35809

DRDMI-YDL

ATTN: DRDMI-R

Ames Research Center

1 Director

ATTN: DAVDL

Moffett Field, CA 94035

Laboratories (AVRADCOM)

Fort Eustis, VA 23604

Applied Technology Laboratory

### DISTRIBUTION LIST

DISTRIBUTION BIST			
No, Copi		No. Copi	
3	Commander US Army Missale Research and Development Command ATTN: DRDMI-CA, Dr. Donald McDaniels DRDMI-EA, Mr. B. Harwell	1	Commander US Army Armament Research and Development Command ATTN: DRDAR-LCB, Mr. M. Dale Watervliet, NY 12189
	DRDMI-TKL, Mr. B. Cobb Redstone Arsenal, AL 35809	1	Commander US Army Arma ent Materiel Readiness mmand
l	Commander US Army Missile Research and Development Command		ATTN: DRE LEP-L, Tech Lib Rock Island, IL 61299
	ATTN: COL Williamson, TOW PM Redstone Arsenal, AL 35809	1	Commandor US Army Training and Doctrine Command
1	Commander US Army Tank Automotive Research & Development Command	d	ATTN: ATCG, Dr. Marvin Pastel Fort Monroe, VA 23651
	ATTN: DRDRA-UL Warren, MI 48090	1	Director US Army TRADOC Systems Analysis Activity
2	Commander US Army Armament Research and Development Command ATTN: DRDAR-TSS		ATTN: ATAA-SL, Tech Lib White Sands Missile Range, NM 88002
	Dover, NJ 07801	4	Commander US Army Infantry Center
5	Commander US Army Armament Research and Development Command ATTN: DRDAR-LC, Dr. J. Frasier DRDAR-LCW, Mr. H. Garver DRDAR-LCF, Mr. F. Saxe		ATTN: ATSH-DCG, BG F. Mahaffey Mr. P. Ferguson Mr. G. Hardgrove ATSH-CD-MSD-F, Mr. Ramsey Fort Benning, GA 31905
	DRDAR-LCU, Mr. A. Moss Mr. T. Malgeri Dover, NJ 07801	2	Director US Army Infantry Center Antiarmor Weapons Special
1	Commander US Army Armament Research and Development Command		Task Force ATTN: DAMO-RQD-I Fort Benning, GA 31905
	ATTN: DRCPM-SA, Mr. J. Brooks Dover, NJ 07801	1	Commandart US Army Armor School

US Army Armor School ATTN: Combat Developments Fort Knox, KY 40121

### DISTRIBUTION LIST

# No. of Copies Organization

- Doputy Under Secretary of the Army for Operations Research ATTN: Mr. David Hardison Washington, DC 20310
- 2 ADTG/DIMIT (J. Constantino; J. Burda) Eglin AFB, FL 32542
- 1 AFATL (Dr. J. R. Mayorsak, Chiof Scientist) Eglin AFB, FL 32542
- 2 Aorojet Bloetro Systems ATTN: Mr. Keith Paradis 1200 W. Hollyvale Street Azusa, CA 91702
- 2 Applied Blectronics Division ATh - Division of Cutler-Hammer ATTN: Mr. Theodore Flattau Melville, L.I., NY 11746
- 2 AVCO Systems Division ATTN: Mr. Thomas Midura 201 Lowell Street Wilmington, MA 01887
- 1 Bolt Boranok & Nowman Inc. ATTN: Mr. Richard Barakat Cambridgo, MA 62138
- 2 Cincinnati Blectronics ATTN: Mr. Robort Seitz Mr. Raymond Schmidt 2630 Glendale-Milford Road Cincinnati, OH 45241
- 2 Environmental Research Institute of Michigan ATTN: Mr. Jerry Beard P.O. Box 8618 Ann Arber, MI 48107

# No. of Coples Organization

- 2 Gonoral Dynamics
  Pomona Division
  ATTN: Mr. L. P. Groon
  P.O. Box 2507
  Pomona, CA 91766
- 2 Honeywoll, Inc. ATTN: Mr. A.C. Hastings Mr. David Erdmann 600 Second Street, North Hopkins, MN 55343
- 2 Hughes Aircraft Company
  Ground Systems Group
  ATTN: Dr. Wesley K. Masenten
  Hr. J. Willner
  P.O. Box 3510
  Fullerton, CA 92634
- 2 Hughes Aircraft Company ATTN: Mr. Ron Sabowski 3100 West Lomita Blvd Torrance, CA 90509
- Martin Marietta Corporation Orlando Division ATTN: Mr. Joseph Stever P.O. Box 5837 Orlando, FL 32855
- 1 Raytheon Company Missilo Systems Division ATTN: Mr. Thomas Crocker Bedford, MA 01730
- 1 Sanders Associates Inc.
  Rederal Systems Group
  ATTN: Mr. Tommy E. Buder,
  NCA1-6228
  95 Canal Street
  Nashua, NH 03063
- 1 SINGER Kearfott Division ATTN: Mr. Hyron Rosenthal 150 Totwa Road Wayne, NJ 07470

#### DISTRIBUTION LIST

# No. of Copies Organization

- 1 System Planning Corporation Suite 1500 ATTN: Dr. James Meni 1500 Wilson Boulevard Arlington, VA 22209
- 1 University of California Lawrence Livermore Laboratory ATTN: Mr. R. Singleton P.O. Box 808 Livermore, CA 94550

## Aberdeen Proving Ground

Dir, USAMSAA
ATTN: Dr. J. Sperrazza
DRDXSY-MP, Mr. H. Gohen
DRXSY-GI, Mr. W. Clifford
DRXSY-DS, Mr. J. Kramar
DRXSY-T, Mr. A. Reid
DRXSY-G, Mr. R. Conroy
Mr. C. Odom

Dir, HEL

ATTN: Mr. J. Torre Mr. G. L. Horley

CDR, USATECOM ATTN: DRSTE-TO-F

Dir, Wpns Sys Concepts Team

Bldg E3516, EA ATTN: DRDAR-ACW

### USER EVALUATION OF REPORT

Please take a few minutes to answer the questions below; tear out this sheet and return it to Director, US Army Ballistic Research Laboratory, ARRADCOM, ATTN: DRDAR-TSB, Aberdeen Proving Ground, Maryland 21005. Your comments will provide us with information for improving future reports.